

I M.Tech - II Semester – Regular Examinations – AUGUST 2018**FINITE ELEMENT METHODS IN ENGINEERING
(MACHINE DESIGN)**

Duration: 3 hours

Max. Marks: 60

Answer the following questions.

1. a) What is Rayleigh-Ritz method? Explain. 7 M

b) Explicate weighted residual method with the help of an example. 8 M

(OR)

2. a) Discuss the basic steps involved in finite element method. 7 M

b) With the help of neat sketches, discuss the node numbering scheme in FEM. 8 M

3. Compute the nodal displacements, stresses and reaction at the support in the stepped bar subjected to an axial loads of $P_1=3000\text{N}$ and $P_2= 2000\text{N}$ as shown in Figure1. The modulus of elasticity of the material of the bar is $2.1 \times 10^5 \text{ MPa}$. 15 M

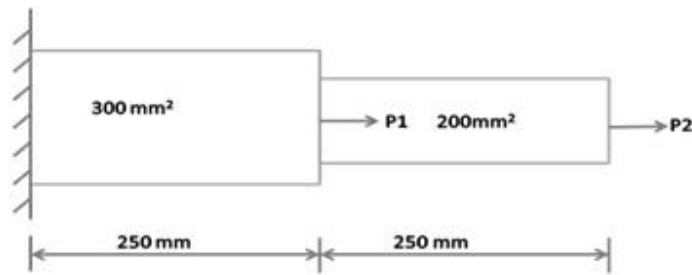


Figure 1

(OR)

4. a) Estimate the stiffness matrix and the deflection at the centre of the simply supported beam of length 3m. A 50 kN of load is acting at the center of the beam. Take flexural rigidity $EI = 800 \times 10^3 \text{ N-m}^2$. 10 M

- b) Derive element stiffness matrix of plane truss element.

5 M

5. a) The nodal coordinates of a triangular element are 1(1,3), 2(5,3) and 3(4,6). At a point P inside the element, the x-coordinates is 3.3 and the shape function $N_1 = 0.3$.

Determine the other shape functions and y-coordinates of the point P. 5 M

- b) An axisymmetric ring element is shown in Figure 2 . Derive the matrices, [B] and [D].

Take $E = 2 \times 10^5 \text{ N / mm}^2$ and $\mu = 0.33$.

10 M

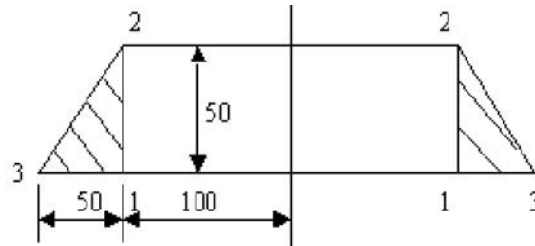


Figure2

(OR)

6. a) Derive the stiffness matrix for a two dimensional four noded isoparametric quadrilateral element. 7 M

b) Evaluate the integral $(2 + x + x^2) dx$ by one point and two point Gaussian quadrature between the limits -1 and +1 and compare with exact value. 8 M

7. Compute the Eigen values and Eigen vectors for the stepped bar shown in Figure3.

$A_1 = 1200 \text{ mm}^2$, $A_2 = 900 \text{ mm}^2$, $E = 200 \text{ GPa}$, $L_1 = 400 \text{ mm}$,
 $L_2 = 300 \text{ mm}$ and mass density = 7840 kg /mm^3 . 15 M

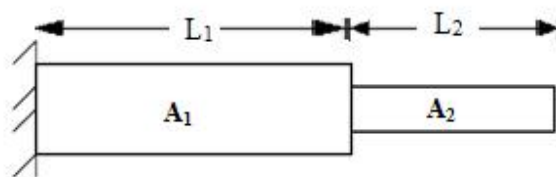


Figure3

(OR)

8. a) Discuss the various convergence requirements used in finite element analysis. 6 M
- b) Compare h-refinement and p- refinement methods. 4 M
- c) What is Pascal's triangle? How it is useful in selecting the polynomials for representing element field variables. 5 M